A Fast Hue-Preserving Histogram Equalization Method for Color Image Enhancement using a Bayesian Framework

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Abstract – In this paper, we introduce a new hue-preserving histogram equalization method based on the RGB color space for image enhancement. We use R -red, G -green, and B -blue $1D$ histograms to estimate the histogram to be equalized using a Naive Bayes rule. The histogram equalization is performed by shift hue-preserving transformations. Our method has linear time and space complexities, which complies with realtime applications requirements. A subjective assessment comparing our method and other three is performed. Experiments showed that our method is more robust than the others in the sense that neither unrealistic colors nor over-enhancement are produced.

1. INTRODUCTION

Image enhancement (IE) techniques have been often applied to Image Processing and Computer Vision applications in order to increase the probability of success in the image analysis task [2]. IE techniques are particularly useful in applications where an image with more distinguished texture details and perceptually better colors are required [3].

A great number of methods can be found in literature for the purpose of IE [3]. Among them, a well-known technique is Histogram Equalization (HE) [2]. HE consists of generating a uniform histogram (*i.e.*, uniform distribution) from an original one. In image processing, the idea of equalizing the histogram of an image is to use the entire range of discrete levels of the image, stretching and/or redistributing the original histogram, such that an enhancement of image contrast is achieved.

In this paper, we introduce a new hue-preserving HE method based on the RGB color space for IE. In fact, the proposed method is an extended and improved version of a previous work [4]. However, instead of using 3D or 2D histograms for IE, as in [5] and [4], we combine $1D$ histograms and a Bayesian framework [1]. Moreover, our method is hue-preserving [6], *i.e.*, neither unrealistic nor new colors are produced after the enhancement process. The new method has linear time complexity with respect to both the image size and the number of discrete levels in each color channels. Hence, its complexity complies with real-time application requirements.

The remainder of this paper is organized as follows. Basic definitions for color images are presented in Section 2. Previous works related to our method are described in Section 3, and in Section 4 our new method is introduced. Experiments are shown in Section 5, and, finally, conclusions are drawn in Section 6.

2. BASIC DEFINITIONS

In this section, we present basic definitions for color images and its probability functions, which will be used throughout this work.

Let N denote the set of natural numbers. Let X be a subset of points $(x, y) \in \mathbb{N}^2$, such that $0 \le x < m$, and $0 \leq y \leq n$, where m and n denote the dimensions of X. Let $||Y||$ denote the cardinality of a set $Y \subseteq \mathbb{N}^2$. Note that $||X|| = m \times n$. A mapping *I*, from *X* to \mathbb{Z}_L^3 , is
called an (color) image (in the *BCB* color space). We called an (*color*) *image* (*in the* RGB *color space*). We denote by I^{RGB} such color image. In real applications, L is typically 256. Indeed, we have three mappings from X to \mathbb{Z}_L , which are the red, green and blue images, *i.e.*, I^R , I^G and I^B . For a point $(x, y) \in X$, $R_i = I^R(x, y)$, $G_i = I^G(x, y)$ and $B_i = I^B(x, y)$, are called the *red*, *green* and *blue levels* of the point (x, y) in *I*, respectively. We can also denote (R_i, G_i, B_i) by I_{R_i, G_i, B_i}^{RGB} . In the following, we
define 1 D 2D and 3D bistograms and probability density define $1D$, $2D$ and $3D$ histograms and probability density and distribution functions for color images.

For the $1D$ case, we first consider the R color channel. Let $H_{R_o}^{I^R}$ be the *absolute frequency* of level R_o in image I^R ,
where $0 \leq R \leq I_0$, in The meaning I^I^R from the layer where $0 \le R_o \le L-1$. The mapping H^{I^R} from the levels of image I^R to its absolute frequency levels, *i.e.*, H^{I^R} : $\mathbb{Z}_L \to \mathbb{N}$, is called the *histogram* of image I^R . Let P^{I^R} be the probability density function of I_1^R . We denote by $P_{R_0}^{I^R}$ the probability of level R_0 , *i.e.*, $P_{R_0}^{I^R} = H_{R_0}^{I^R}/m \times n$, where $0 \le R_o \le L-1$. Let C^{I^R} be the cumulative density function (CDE or the probability distribution function) of function (CDF, or the probability distribution function) of *IR*. We denote by $C_{R_o}^{I^R}$ the cumulative density of level R_o , *i.e.*, $C_{R_o}^{I^R} = \sum_{r_o=0}^{R_o} P_{r_o}^{I^R}$, where $0 \le R_o \le L - 1$. It is immediate to extend the above definitions of I^R image, *i.e.*, H^{I^R} , P^{I^R} and C^{I^R} , to I^G and I^B images.

For the 2D case, we first consider the R and G color

channels. Let H_{R_i,G_i}^{IG} be the *absolute frequency* of R_i and G_i colors, in image I^{RG} . The mapping H^{IG} from the levels of image I^{RG} to its absolute frequency levels, the levels of image I^{RG} to its absolute frequency levels, *i.e.*, $H^{I^{RG}}$: $\mathbb{Z}_L^2 \rightarrow \mathbb{N}$, is called the *histogram* of image I^{RG} . Let $P^{I^{RG}}$ be the probability density function of I^{RG} . We denote by $P_{R_i,G_i}^{I^{RG}}$ the probability of (R_i, G_i) , *i.e.*,
 $P_{R_i,G_i}^{I^{RG}} = H_{R_i,G_i}^{I^{RG}}/m \times n$. Let $C^{I^{RG}}$ be the CDF of I^{RG} . We denote by C_{R_i,G_i}^{IRG} the cumulative density of (R_i, G_i) ,
i.e., $C_{R_i,G_i}^{IRG} = \sum_{r_i=0}^{R_i} \sum_{g_i=0}^{G_i} P_{r_i,g_i}^{IRG}$. It is immediate to extend the above definitions of I^{RB} image, *i.e.*, H^{IRG} , $P^{I^{RG}}$ and $C^{I^{RG}}$, to I^{RB} and I^{GB} images.

For the 3D case, we have a single histogram and probability functions to be defined. Let H_{R_i,G_i,B_i}^{RGB} be the absolute frequency of R_i , G_i and R_i colors in image I *absolute frequency* of R_i , G_i and B_i colors in image I.
Note that $H_{R_i,G_i,B_i}^{RGB} = 0$ if there is no $(x, y) \in X$ such that $H_{R_i,G_i,B_i}^{RGB} = (R, G, R)$. The majority $H_{R_i}^{RGB}$ that $I^{RGB}(x, y) = (R_i, G_i, B_i)$. The mapping H^{IBGB} from the levels of image I to its absolute frequency levels, *i.e.*, $H^{I^{RGB}}$: $\mathbb{Z}_{L}^{3} \rightarrow \mathbb{N}$, is called the *histogram* of image I^{RGB} . Let $P^{I^{RGB}}$ be the probability density function of I^{RGB} . We denote by $P_{R_i,G_i,B_i}^{I^{RGB}}$ the probability of (R_i, G_i, B_i) , *i.e.*, $P_{R_i, G_i, B_i}^{I^{RGB}} = H_{R_i, G_i, B_i}^{I^{RGB}} / m \times n$. Let $C^{I^{RGB}}$ be the CDF of I^{RGB} . We denote by $C^{I^{RGB}}_{R_i, G_i, B_i}$
the cumulative density of (R_i, G_i, B_i) , *i.e.*, $C^{I^{RGB}}_{R_i, G_i, B_i} = \sum_{r_i=0}^{R_i} \sum_{g_i=0}^{G_i} \sum_{b_i=0}^{B_i} P^{I^{RGB}}_{r_i, g_i, b_i}$.

In the next section, we present previous works related to the proposed method.

3. PREVIOUS WORKS

In this section we present works directly related to our proposed method. We first briefly describe the classical HE method for gray-level IE, which is extended for color images. We then show the $3D$ HE method proposed by Trahanias and Venetsanopoulos in [5], which is followed by a description of a 2D HE method recently proposed by us in [4]. These descriptions will help us to introduce our method in Section 4.

3.1 Classical 1^D *Histogram Equalization*

In this section we describe the HE method for monochrome images (*e.g.*, gray-level or red ones), followed by its extension to deal with I^{RGB} images. The goal of HE is to uniformly distribute H^{I^R} over the entire range of levels or, equivalently, to generate a CDF which increases monotonically as a straight line, such that an image contrast enhancement be achieved.

The HE method for monochrome images is described as follows. Let I and O be the input and the output images, or the original and the equalized images, respectively. Let H^{I^R} , P^{I^R} and C^{I^R} be defined as in Section 2. Let H^{O^R} be the desired uniform histogram of the output image, where any level l has the same amount of pixels, *i.e.*, $H_1^{OR} = \frac{1}{L}(m \times n)$, or the same density, *i.e.*, $P_1^{OR} = 1/L$.
Thus, the CDE C_1^{OR} is defined in function of l as C_1^{OR} . Thus, the CDF C^{O^R} is defined in function of l as $C_l^{O^R} = \sum_{i=0}^l P_i^{I^R} = (l+1)/L$.
The l' output equalized level corresponding to the input

The l' output equalized level corresponding to the input level l is obtained as the one that minimizes the difference

between $C_{l'}^{O^R}$ and $C_{l}^{I^R}$. In other words, the output level l' for the input level l can be computed as the transformation for the input level l can be computed as the transformation function $T^{I^R}(l)$, *i.e.*, $l' = T^{I^R}(l) = |(L - 1) \times C_l^{I^R}|$, where $|z|$ stands for the percept integer to z . To generate where $|z|$ stands for the nearest integer to z. To generate the output enhanced image with this transformation, for any pixel $(x, y) \in X$, we obtain the output value $O^R(x, y)$ as $l' = T^{I^R}(l)$, where $l = I^R(x, y)$.

This method can easily be extended for color IE, by applying separately the equalization process described above to each I^R , I^G and I^B images. This extended method produces a well-known problem; it produces unrealistic colors, since it is not hue preserving [6]. In the following, we call this extended method as the classical 1D HE for color IE.

3.2 3^D *Histogram Equalization*

The method proposed by Trahanias and Venetsanopoulos [5] takes into account the correlation of the three channels, R, G, and B, simultaneously. And it can can be described as follows.

Let I and O be the input and output color images. Let $H^{I^{RGB}}$, $P^{I^{RGB}}$ and $C^{I^{RGB}}$ be defined as in Section 2. Let $H^{O^{RGB}}$ be the uniform histogram of the output image, where any entry (R_o, G_o, B_o) has the same amount of pixels, since a such output histogram is desired, *i.e.*, $H_{R_o,G_o,B_o}^{QRGB} = \frac{1}{L^3}(m \times n)$, or the same density, *i.e.*,
 $P_{R_o,G_o,B_o}^{ORGB} = 1/L^3$. And so, any entry (R_o, G_o, B_o) in $C^{O^{RGB}}$ can be directly computed using its values R_o , G_o and ^Bo, *i.e.*,

$$
C_{R_o,G_o,B_o}^{O^{RGB}} = \frac{(R_o+1)(G_o+1)(B_o+1)}{L^3}.
$$
 (1)

To produce the output enhanced image, for any input pixel $(x, y) \in X$, where $(R_i, G_i, B_i) = I^{RGB}(x, y)$, the smallest (R_o, G_o, B_o) is found for which the inequality

$$
C_{R_i,G_i,B_i}^{I^{RGB}} - C_{R_o,G_o,B_o}^{O^{RGB}} \ge 0,
$$
\n(2)

is true. However this step presents an ambiguity since there exist many solutions for (R_o, G_o, B_o) that satisfy Equation 2. This ambiguity is remedied as follows. The computed value of $C^{I^{RGB}}$ at (R_i, G_i, B_i) is initially com-
pared to the value of $C^{O^{RGB}}$ at (R_o, G_o, B_o)). If $C^{I^{RGB}}$ is greater (*resp.* less) than C^{ORGB} , then the indexes R_o , C_{o} and B_{o} representedly increased (*resp. degreesed*). ^Go, and ^Bo are repeatedly increased (*resp.* decreased), one at a time, until Equation 2 is satisfied. The obtained (R_o, G_o, B_o) is the output entry to (R_i, G_i, B_i) , *i.e.*, if $(x, y) \in x$ and $(R_i, G_i, B_i) = I^{RGB}(x, y)$, then $O^{RGB}(x, y)=(R_o, G_o, B_o).$

3.3 2^D *Histogram Equalization*

In this section, we describe the 2D HE method for Color IE, which is published in [4]. In this method, instead to use the correlation among the three channel as [5], it is used the correlation of channels two at a time. The method is described as follows.

Let I and O be the input and output images. Let the input 2D histograms and probability functions be defined

Figure 1. Results for the beach (partial Brazilian flag) image: (a) original image; (b) 1D HE; (c) 3D HE; (d) 2D HE; (e) our proposed method.

as in Section 2. Indeed, in this method, we do not equalize the three $2D$ histogram, but we equalize a $3D$ pseudohistogram, $H^{I^{RGB}}$, which is defined based on a pseudo $3D$ CDF. This CDF, ${C'}^{I^{RGB}}$, is computed as the product of the three 2D CDFs for any entry (R_i, G_i, B_i) , *i.e.*,

$$
C'_{R_i, G_i, B_i}^{I^{RGB}} = C_{R_i, G_i}^{I^{RG}} \times C_{R_i, B_i}^{I^{RB}} \times C_{G_i, B_i}^{I^{GB}}.
$$
 (3)

The main rationale for computing this pseudo-CDF as the product of three 2D CDFs is that the three channels in an image are usually not simultaneously correlated.

The output entry (R_o, G_o, B_o) for any pixel $(x, y) \in X$
is computed as follows. Initially, (R_o, G_o, B_o) (the output is computed as follows. Initially, (R_o, G_o, B_o) (the output
triplot) is set up as $(P, G, B) = IRGB(a, a)$. Then an triplet) is set up as $(R_i, G_i, B_i) = I^{RGB}(x, y)$. Then an initial $C_{R_o,G_o,B_o}^{Q_{RGB}}$ is computed by Equation 1, and an error is produced, *i.e.*,

$$
C'_{R_i, G_i, B_i}^{I^{RGB}} - C_{R_o, G_o, B_o}^{O^{RGB}}.
$$
 (4)

This error will be used to guide the iterative process increasing or decreasing the output triplet (R_0, G_0, B_0) . Note that as in [5], the solution for Equation 4 also presents an ambiguity. There are several solutions for (R_o, G_o, B_o) that satisfy Equation 1. Instead to increase or decrease each channel at a time by a unit, the channels are increasing or decreasing by proportional factors based on each channel (for details, see [4]). The rationale for this is that we can stretch the histogram simultaneously in all three direction by factors depending on their-self. The output triplet (R_o, G_o, B_o) is the nearest integer triplet which approximates to zero the difference between the CDFs $C^{i\overline{I}^{RGB}}$ and $C^{iO^{RGB}}$, *i.e.*, Equation 4.

Note that this HE method is not hue preserving, since the shift transformation performed from (R_i, G_i, B_i) to $(R_i +$ $k \times T_R$, $G_i + k \times T_G$, $B_i + k \times T_B$) $\approx (R_o, G_o, B_o)$ is not hue preserving [6], where T_R , T_G and T_B stands for the displacement taken for each channel and k is the number of iterations required to find the miminum error in Equation 4. The hue is not preserved because we may take different displacements in each directions.

In the next section, we present our proposed method.

4. THE PROPOSED METHOD

In this section, we present a hue-preserving HE method based on the RGB color space for IE. Indeed, this method is an extended and improved version of the method proposed in Section 3.3. It is linear with respect to both the image size and the number of discrete levels in each channel.

The method is based on the independence assumption of color channels, which is used in a Bayesian framework for computing the CDF. In Data Mining and Knowledge Discovery domains, it is well known that Bayesian classifiers work well, even though the independence assumption is violated [1]. Although it is also well known that this assumption does not hold for the R , G and B channels of color images, we hope that the enhancement produced in color image through HE will work well. We use 1D histograms to estimate a 3D probability distribution function, and then equalize the conceived histogram through the estimated function. The method is described as follows.

Let I and O be the input and the output images, respectively. Let H^{I^R} , H^{I^G} , H^{I^B} , P^{I^R} , P^{I^G} , P^{I^B} , $C_{rel}^{I^R}$ C^{I^G} and C^{I^B} be defined as in Section 2. The CDF $C^{I^{RGB}}$ for any entry (R_i, G_i, B_i) can be estimated as the product of every cumulative distribution $C_{R_i}^{I^B}$, $C_{G_i}^{I^G}$, and $C_{B_i}^{I^B}$, following the rule, *i.e.*,

$$
C'_{R_i, G_i, B_i}^{I^{RGB}} = C_{R_i}^{I^R} \times C_{G_i}^{I^G} \times C_{B_i}^{I^B}.
$$
 (5)

Note that in this equation, ${C'}^{I^{RGB}}$ obeys a Naive Bayes sense, whilst in Equation 3 $C^{I^{RGB}}$ is defined without a mathematical mean. Unlike to iteratively increase or decrease R_o , G_o and B_o , in order to minimize Equation 4 as performed in the method described in Section 3.3, we propose to find the output triplet (R_o, G_o, B_o) for any image pixel in a single step, *i.e.*, O(1). From Equations 4 and 1 or for solving Equation 5, we have

$$
C'_{R_i, G_i, B_i}^{I^{RGB}} - \frac{(R_o + 1)(G_o + 1)(B_o + 1)}{L^3} = 0.
$$
 (6)

If we take R_o , G_o and B_o as $R_i + k$, $G_i + k$ and $B_i + k$, respectively, where k is the number of iterations required for minimizing Equation 4, we obtain

$$
k^{3} + k^{2}[R'_{i} + G'_{i} + B'_{i}] +
$$

\n
$$
k[R'_{i} \times G'_{i} + R'_{i} \times B'_{i} + G'_{i} \times B'_{i}] +
$$

\n
$$
R'_{i} \times G'_{i} \times B'_{i} - L^{3} \times C'_{R_{i}, G_{i}, B_{i}} = 0.
$$
\n(7)

where R'_i , G'_i , and B'_i means $R_i + 1$, $G_i + 1$, and $B_i + 1$, respectively. By solving this a cubic equation in function respectively. By solving this a cubic equation in function of k, we obtain the desired output triplet (R_o, G_o, B_o) as the input one plus the displacement k, *i.e.*, $(R_i + |k|, G_i +$ $|k|, B_i + |k|$, where $|k|$ stands for the nearest integer to k . Equation 7 can easily be solved by Nickalls [7] or by classical Cardian methods using transcendental functions. It would be preferred to use the Nickalls method, since it is faster and mathematically simpler than the last one.

Figure 2. Results for the train image: (a) original image; (b) 1D HE classic; (c) 3D HE; (d) 2D HE; (e) our proposed method.

Note that any image pixel is equalized following a shift transformation by a k factor, *i.e.*, (R_i, G_i, B_i) to $(R_i +$ $|k|, G_i + |k|, B_i + |k|$, which is hue preserving [6]. Hence the proposed method is also hue preserving.

5. EXPERIMENTS

In this section, a comparison among our proposed HE method and the $1D$ [2], the $3D$ [5], and the $2D$ [4] methods is carried out. A subjective assessment is carried out to compare the visual quality of the images. Here we discuss results for two images.

Figure 1 shows the results for the first image, the beach. Note that unrealistic colors are present in the image generated by the $1D$ HE method (Figure 1(b)). The image produced by the 3D HE method is overenhanced, producing colors very saturated (Figure 1(d)), *i.e.*, bright colors. In turn, the image produced by the 2D HE method (Figure 1(d)) is more realistic than the others. In contrast, another type of judgement can be performed considering the application. We can say that the resulted image of the 3D HE method has better quality than the others, since the water region in the image was better enhanced. Despite of these arguments, we can say that our method generates an image (Figure $1(e)$) with a good balance between non saturated and realistic colors.

Figure 2 shows the results for the second image, the train. We observe that the $3D$ HE method produces an overenhanced image (Figure $2(c)$), that is, the colors are very saturated. Our method and the 2D one produce images (Figure 2(d)) better enhanced than the one obtained by the 3D HE method. However, some hidden details in dark regions continue to be uncleared. In our opinion, the best enhancement is achieved by the image produced by the 1D HE method (Figure 2(b)). In this case, the image produced by the 1D HE method presents colors which are more realistic for the green regions and have more details than those produced by the other three methods. However, again, note that in the sky portion of the image, unrealistic colors are produced by the 1D HE method.

From the discussion above, we claim that our method produces images (Figures 1(e) and $2(e)$) with the best tradeoff between the enhanced colors and saturation. That is, our method produces images with colors that are more realistic than the 1D and 2D HE methods (which are not hue preserving), and the images are not so saturated as the ones produced by the 3D HE method.

6. CONCLUSION

In this paper, we introduced a new hue-preserving HE method based on the RGB color space for IE. The proposed method has $O(max(m \times n, L))$ and $O(L)$ time and space complexities, respectively. Such method complies with real-time application requirements, given its complexities.

Although the classical $1D$ HE method is six times faster than ours, it is not hue preserving. Remark that our method is two and forty times faster than the 2D and 3D HE ones, respectively. In practice, our method enhances 1024×1024 image pixels in 100 milliseconds on a Pentium 4 - 2GHz.

As shown on the experiments in the previous section, it is difficult to judge an enhanced image result even with a subjective assessment. However, we claim that our method is more robust than the others in the sense that neither unrealistic colors nor overenhanced are produced. For future works, we plan to evaluate the methods using naturalness and colorfulness metrics [8] on a database with hundreds of images collected from internet, such that a quantitative comparison can be performed.

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REFERENCES

- [1] P. Domingos and M. Pazzani, "On the optimality of the simple bayesian classifier under zero-one loss," *Machine Learning*, vol. 29, no. 2-3, pp. 103–130, 1997.
- [2] R. Gonzalez and R. Woods, *Digital Image Processing*, 2nd ed. Prentice Hall, Jan. 2002.
- [3] K.-Q. Huang and Q. Wang and Z.-Y. Wu, "Natural color image enhancement and evaluation algorithm based on human visual system," *Computer Vision and Image Understanding*, vol. 103, pp. 52–63, 2006.
- [4] D. Menotti, A. P. Melo, A. de Albuquerque Araújo, J. Facon, and E. M. Sgarbi, "Color image enhancement throught 2D histogram equalization," in *13th IWSSIP*, Budapest, Hungry, 21-23 September 2006, pp. 235–238.
- [5] P. Trahanias and A. Venetsanopoulos, "Color image enhancement through 3-d histogram equalization," in *Proceedings of 11th International Conference on Pattern Recognition (ICPR)*. IEEE, 1992, pp. 545–548.
- [6] S. Naik and C. Murthy, "Hue-preserving color image enhancement without gamut problem," *IEEE Tran. on Image Processing*, vol. 12, no. 12, pp. 1591–1598, Dec. 2003.
- [7] R. Nickalls, "A new approach to solving the cubic: Cardan's solution revealed," *The Mathematical Gazette*, vol. 77, pp. 354–359, 1993.
- [8] S. Yendrikhovskij, F. Blommaert, and H. de Ridder, "Perceptually optimal color reproduction," in *Proc. of SPIE: Human Vision and Elec. Imag. III*, vol. 3299, 1998, pp. 274–281.